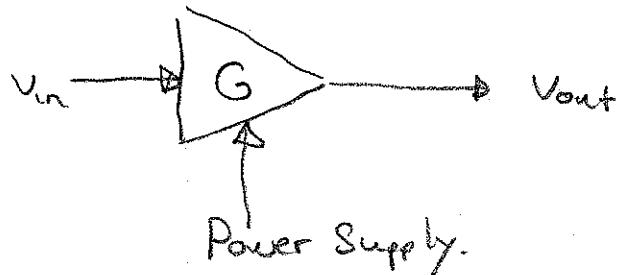
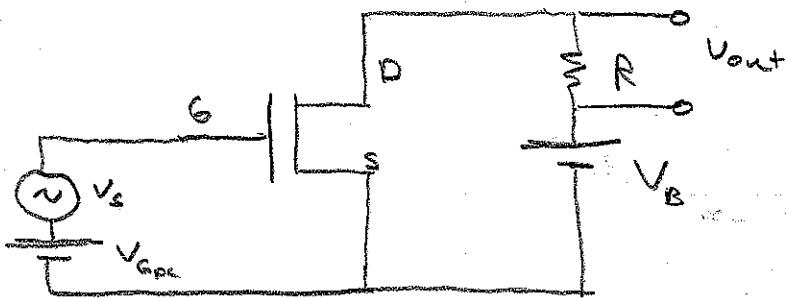


Amplifier 1 dB compression Pt & 3rd Order Intercept.

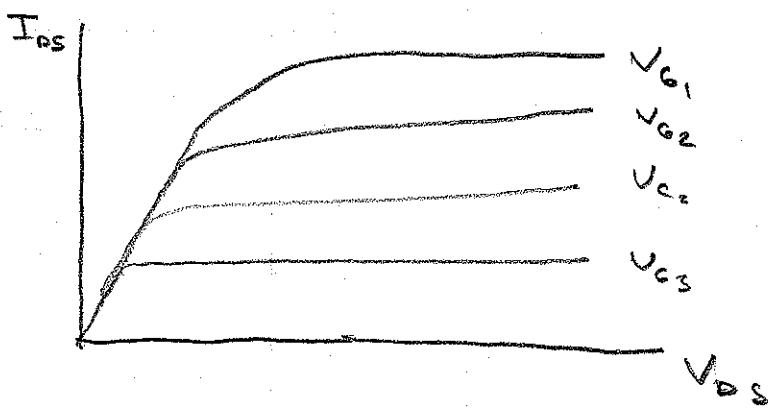


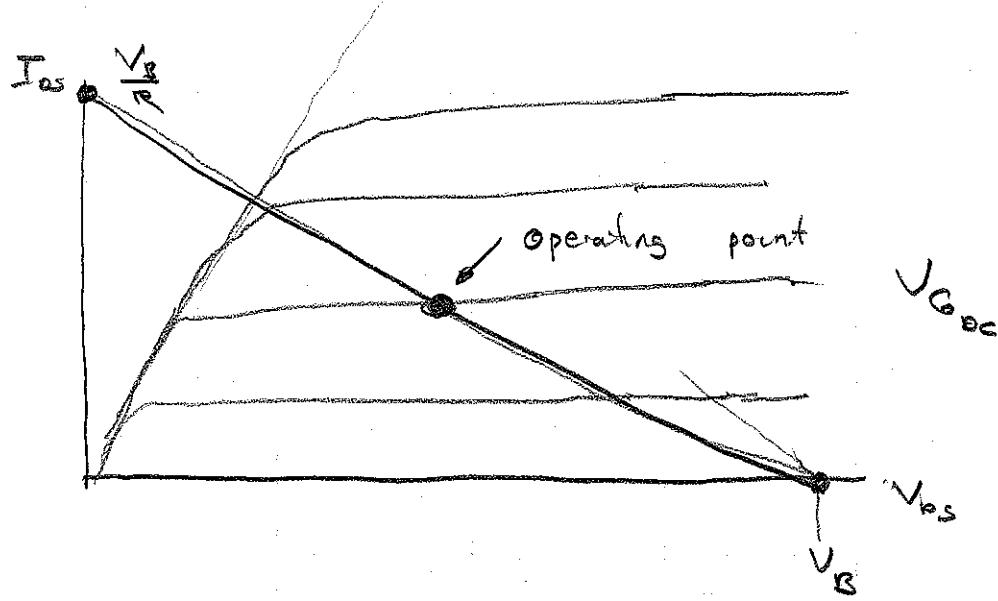
If there is a finite amount of power available from the power supply then there are limits to how large V_{out} can be.



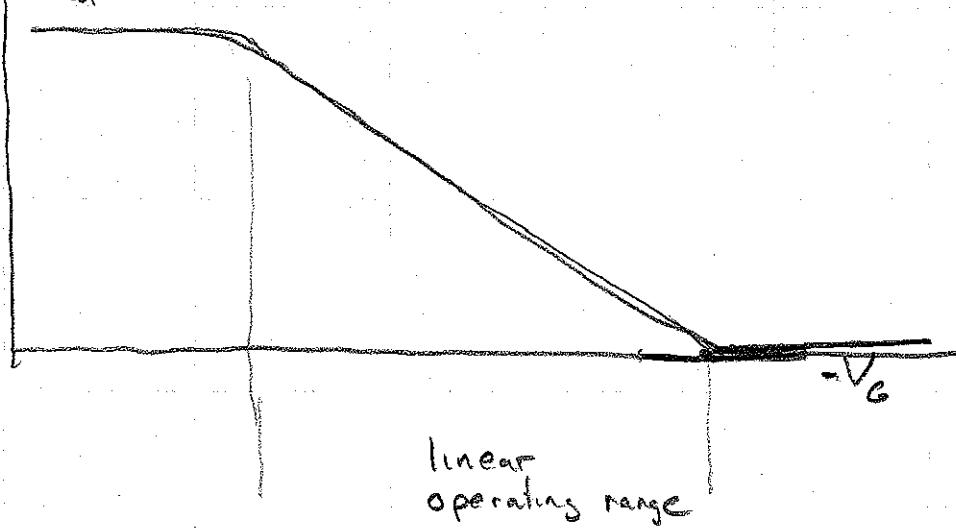
$$V_{ds} = V_B - I_{ds} R$$

FET V-I curve

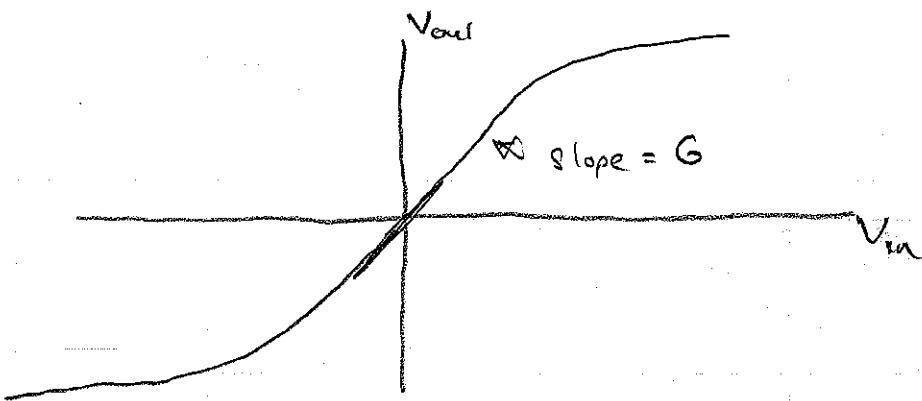




$$V_{out} = I_{D_s} R$$



Remove the bias for the time being.
We can model a gain curve as



We can expand gain curve as a Taylor series

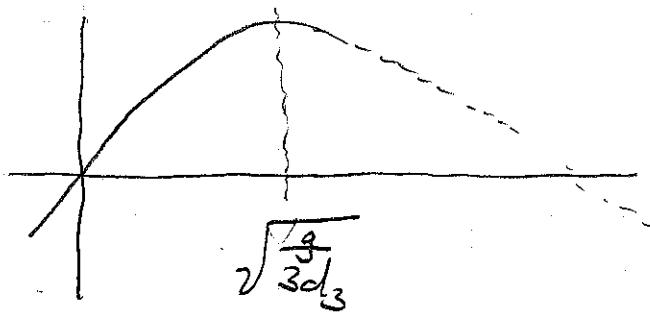
$$V_{out} = \sqrt{g V_{in}} + g V_{in} - \frac{d_2}{2} V_{in}^2 - \frac{d_3}{3} V_{in}^3 \dots$$

AC coupled odd about V_{in}

multi sign gain roles over

For the time being, ignore $d_n > d_3$

$$V_{out} = g V_{in} - d_3 V_{in}^3$$



$$V_{in_{max}}^2 = \frac{g}{3d_3}$$

$$V_{max}^2 = \frac{g}{3d_3}$$

$$d_3 = \frac{g}{3V_{max}^2}$$

$$V_{out} = g \left(V_{in} - \frac{V_{in}^3}{3V_{max}^2} \right)$$

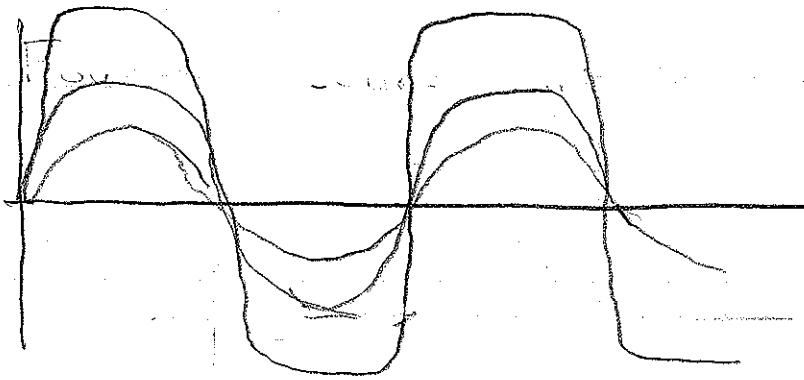
$$\text{Let } V_{in} = V_i \cos \omega t$$

$$\begin{aligned}\cos^3 x &= \cos x \cos^2 x \\ &= \cos x \left(\frac{1}{2} \cos 2x + \frac{1}{2} \right) \\ &= \frac{1}{2} \cos x \cos 2x + \frac{1}{2} \cos x \\ &= \frac{1}{2} \left(\frac{1}{2} \cos x + \frac{1}{2} \cos 3x \right) + \frac{1}{2} \cos x \\ &= \frac{3}{4} \cos x + \frac{1}{4} \cos 3x\end{aligned}$$

$$V_{out} = g V_i \cos \omega t - \frac{g V_i^3}{3V_{max}} \left(\frac{3}{4} \cos \omega t + \frac{1}{4} \cos 3\omega t \right)$$

$$\begin{aligned}V_{out} &= g \left(1 - \left(\frac{V_i}{2V_{max}} \right)^2 \right) V_i \cos \omega t \\ &\quad - \frac{g}{3} \left(\left(\frac{5V_i}{22V_{max}} \right)^2 \right) V_i \cos 3\omega t\end{aligned}$$

Non-linearities generate harmonics !!



$$f(t) = \sum_{n=1}^{\infty} c_n \sin n\omega_0 t$$

$$c_n = \frac{4}{T} \int_0^{T/2} f(x) \sin n \frac{2\pi}{T} t + dt$$

for square wave

$$c_n = \frac{4}{T} \int_0^{T/2} \sin \frac{2\pi n}{T} t + dt$$

$$= -\frac{4}{T} \frac{1}{2\pi n} (\cos \pi n - 1)$$

$$= \frac{4}{\pi n} \text{ for } n \text{ odd}$$

$$= 0 \text{ for } n \text{ even.}$$

$$f(t) = \sum_{n=1}^{\infty} \frac{4}{\pi(2n-1)} \sin((2n-1)\omega_0 t)$$

↑
1 over n
n odd

1 dB compression point.

Gain at the fundamental at low power

$$g_{\text{low}} = g$$

Gain at the fundamental at high power

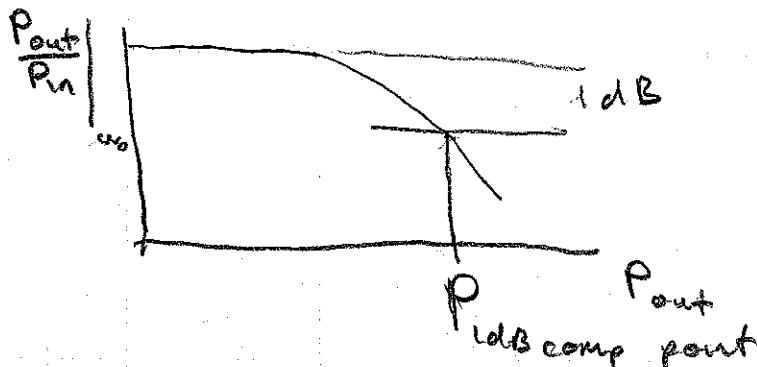
$$g_{\text{high}} = g \left(1 - \left(\frac{V_i}{2V_{\max}} \right)^2 \right)$$

$$\frac{g_{\text{high}}}{g_{\text{low}}} = \left(1 - \left(\frac{2V_i}{2V_{\max}} \right)^2 \right)$$

$$10 \log \left(\frac{(g_{\text{high}})^2}{g_{\text{low}}} \right) = -1 \text{dB}$$

is defined as the 1 dB compression point

Power at which the power gain at the fundamental at high power is 1 dB lower than the power gain at zero power



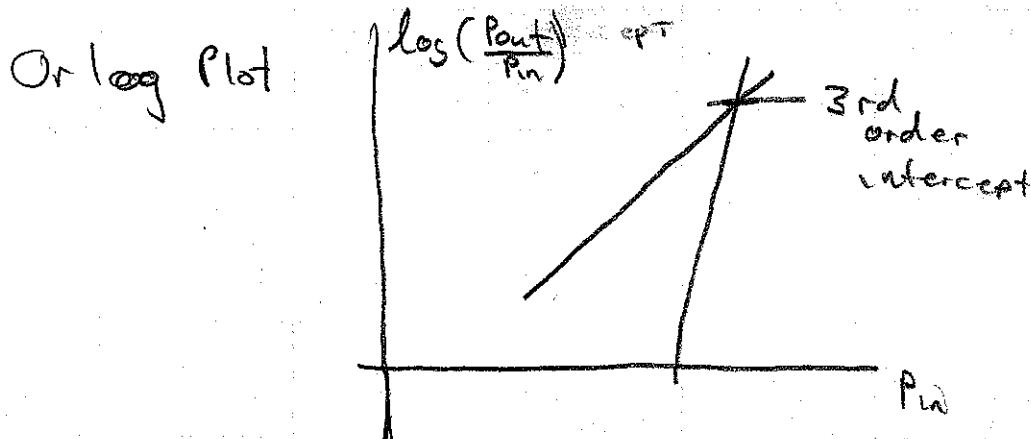
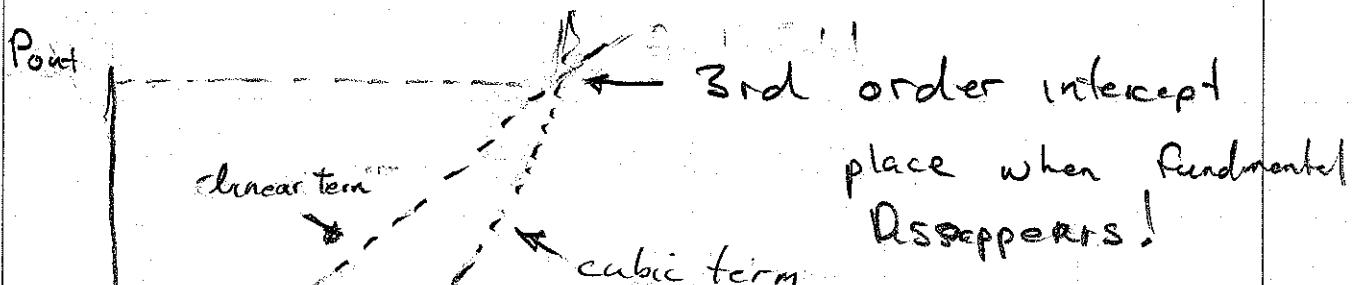
$$-1 \text{ dB} \Rightarrow 10^{-\frac{1}{10}} = (0.794)$$

$$\left(\frac{V_{out}}{V_{in}} - \left(\frac{V_i}{2V_{max}} \right)^2 \right)^2 = .794$$

$$\left(1 - \left(\frac{V_i}{2V_{max}} \right)^2 \right) = .891$$

$$V_i = .66 V_{max} \text{ (for our simple model)}$$

3rd Order Intercept



Never really go to the 3rd order intercept \Rightarrow usually past the destroy level of the amplifier

3rd order intercept

$$k = \left(\frac{V_i}{2V_{max}} \right)^2 = 0$$

$$V_i = 2V_{max}$$

$$20 \log_{10} \left(\frac{V_i|_{\text{intercept}}}{V_i|_{-10\text{dBcomp}}} \right) = 9.63 \text{ dB}$$

\therefore 3rd order intercept $\approx 10 \text{ dB}$
greater than the 1dB compression point.

3rd order Inter modulation Distortion.

$$\underline{v}_m = \underline{v}_1 \cos((\omega_0 + \Delta\omega)t) + \underline{v}_2 \cos((\omega_0 - \Delta\omega)t)$$

$$v_{out} = g \left(v_m - \frac{\underline{v}_m^3}{3V_{max}^2} \right)$$

$$(\underline{v}_1 + \underline{v}_2)^3 = \underline{v}_1^3 + 3\underline{v}_1^2 \underline{v}_2 + 3\underline{v}_1 \underline{v}_2^2 + \underline{v}_2^3$$

$$\underline{v}_1^3 = \frac{3}{4} \cos((\omega_0 + \Delta\omega)t) + \frac{1}{4} \cos(3(\omega_0 + \Delta\omega)t)$$

$$\underline{v}_2^3 = \frac{3}{4} \cos((\omega_0 - \Delta\omega)t) + \frac{1}{4} \cos(3(\omega_0 - \Delta\omega)t)$$

$$\underline{v}_1^2 \underline{v}_2 = \frac{1}{2} (1 + \cos 2(\omega_0 + \Delta\omega)t) \cos((\omega_0 - \Delta\omega)t)$$

$$= \frac{1}{2} \cos((\omega_0 - \Delta\omega)t)$$

$$+ \frac{1}{4} \cos(3\omega_0 + \Delta\omega)t + \frac{1}{4} \cos(\omega_0 + 3\Delta\omega)t$$

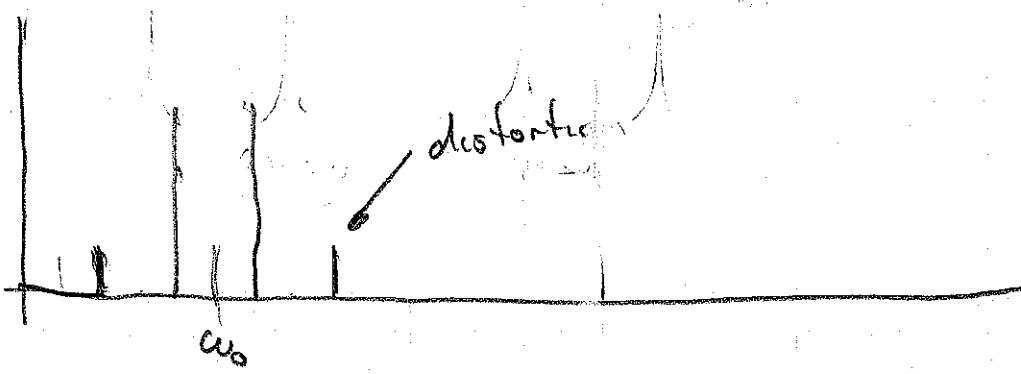
$$\underline{v}_1 \underline{v}_2^2 = \frac{1}{2} \cos((\omega_0 + \Delta\omega)t)$$

$$+ \frac{1}{4} \cos(3\omega_0 - \Delta\omega)t + \frac{1}{4} ((\omega_0 - 3\Delta\omega)t)$$

Let

$$v_i = v_0 \cos((\omega + \Delta\omega)t) + v_0 \cos((\omega - \Delta\omega)t)$$

Assume $\Delta\omega$ small



Amplitude of distortion products

$$= \frac{g}{3 V_{max}^2} \cdot \frac{3}{4} (v_0)^3$$

$$= g v_0 \left(\frac{v_0}{2 V_{max}} \right)^2$$

When $v_0 = 2V_{max}$, the amplitude of the distortion products match the linear power

② To measure 3rd order intercept

- 1) Create two tones of same amplitude but different frequencies
- 2) Increase tone amplitude & measure distortion product compared to tone amplitude on a spectrum analyzer
- 3) Extrapolate when distortion products will match linear signal

